

More

Resonances and Excited States

Particles that are unstable against decay by the strong interaction have mean lives of the order of 10^{-23} s and therefore cannot be detected by ordinary means. For example, if such a particle moves with nearly the speed of light, it can travel a distance of only about $r = c\tau = (3 \times 10^8 \text{ m/s})(10^{-23} \text{ s}) = 3 \times 10^{-15} \text{ m} = 3 \text{ fm}$ (about the diameter of a nucleus), far too short to leave a track in a spark or time projection chamber. The existence of such particles is inferred from *resonances* in the scattering cross sections of one hadron on another, or from the energy distribution of nuclear reaction products. This process is the nuclear analogue of the atomic Franck-Hertz effect described in Section 4-5.

Figure 13-16 shows the cross section σ versus energy for the scattering of π^+ and π^- mesons by protons. There is a strong resonance in the cross section at a π^+ kinetic energy of 195 MeV (in the laboratory frame). This corresponds to a total energy in the center-of-mass frame (including the rest energies of the π^+ and p) of 1232 MeV. The width of this resonance in the CM frame is about 100 MeV, which corresponds to a lifetime of the state of the order of $\tau = \hbar/\Delta E \approx 10^{-23}$ s. Despite the brief lifetime of this resonance state, such a state is now considered to be a particle that is in many ways as fundamental as those in Table 13-1 which are stable against hadronic decay. The particle is designated as $\Delta^{++}(1232)$. It has zero strangeness, since both p and π have zero strangeness. Furthermore, the isospin is $3/2$, since $T = 1/2$ and $T_3 = +1/2$ for the proton and $T = 1$ and $T_3 = +1$ for the π^+ . The spin and parity can be inferred from angular distribution measurements. The $\Delta(1232)$

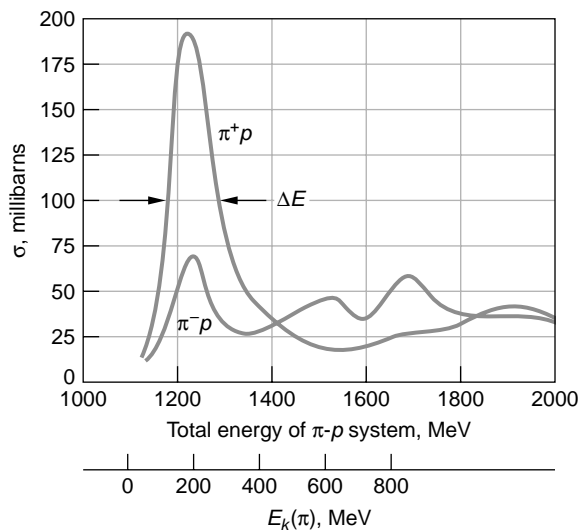


Fig. 13-16 Cross section for scattering of π^+ and π^- mesons by protons. The resonance at a pion energy of 195 MeV, corresponding to a total center-of-mass energy (including rest energy) of 1232 MeV, indicates the existence of a new particle called the Δ particle. Other resonances in the $\pi^- + p$ scattering indicate other particles of greater rest energy. ΔE is the width of the curve at half the peak height.

Continued

In Equation 13-31 the second-step pions correspond to the particle C in the above discussion. The Σ^\pm are the unseen particle E . The energy balance yields its mass. Table 13-6 lists some of the mesons and baryons that are unstable to decay via the strong interaction. Many more have been discovered, some of whose properties are not yet completely established.

Example 13-9 Lifetime of $\Lambda(1520)$

From the width of the resonance of the $\Lambda(1520)$ given in Table 13-6 estimate the lifetime of the particle.

Solution

The width (ΔE) tabulated in the table is the full width at half of the maximum height of the $\Lambda(1520)$ resonance curve similar to that of the Δ shown in Figure 13-16. From the table the value is 16 MeV. The lifetime of the $\Lambda(1520)$ is then given by

$$\tau = \frac{\hbar}{\Delta E} = \frac{1.055 \times 10^{-34} \text{ J} \cdot \text{s}}{(16 \text{ MeV})(1.60 \times 10^{-13} \text{ J/MeV})} = 4.1 \times 10^{-23} \text{ s}$$

Example 13-10 Decay of the $\Sigma^+(2030)$

The positively charged $\Sigma(2030)$ listed in Table 13-6 decays according to the reaction $\Sigma^+ \rightarrow N^+ + \bar{K}^0$. Which of the N resonances in the table can be reached by this decay? What will be the combined energies of the N^+ and \bar{K}^0 in each case?

Solution

The mass of the $\Sigma(2030)$ is $2030 \text{ MeV}/c^2$ and that of the \bar{K}^0 (from Table 13-1) is $498 \text{ MeV}/c^2$. Thus, any N resonance can be reached whose mass is given by

$$\text{Mass}(N) \leq \text{mass}(\Sigma) - \text{mass}(\bar{K}^0)$$

$$\text{Mass}(N) \leq 2030 - 498 = 1532 \text{ MeV}/c^2$$

Only one N resonance in Table 13-6 has a mass less than this amount, the $N(1470)$.

The combined kinetic energy of the decay products is then

$$E_k = 2030 \text{ MeV} - 1470 \text{ MeV} = 560 \text{ MeV}$$